

HW Review:

#56: $m = 1000 \text{ kg}$ $t = 10 \text{ s}$

$\rightarrow +$ $v_i = 20 \text{ m/s}$ $v_f = 0 \text{ m/s}$

 $F = ?$

$$F \Delta t = m(v_f - v_i)$$

$$F = \frac{m(v_f - v_i)}{\Delta t}$$

$$= \frac{(1000 \text{ kg})(0 \text{ m/s} - 20 \text{ m/s})}{10 \text{ s}}$$

$$= -2000 \text{ N}$$

#57: $\rightarrow +$



$$m_1 = 2 \text{ kg} \quad m_2 = 2 \text{ kg}$$

$$v_{1i} = 3 \text{ m/s} \quad v_{2i} = 0 \text{ m/s} \quad v_f = ?$$

This is an **inelastic** collision.

$$\vec{p}_{1i} + \vec{p}_{2i} = \vec{p}_{\text{total final}}$$

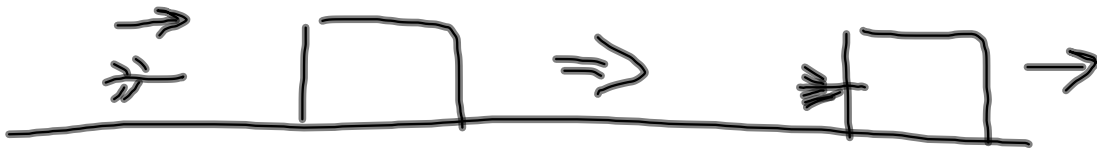
$$m_1 v_{1i} + m_2 v_{2i} = (m_1 + m_2) v_f$$

$$v_f = \frac{m_1 v_{1i}}{m_1 + m_2}$$

$$= \frac{(2 \text{ kg})(3 \text{ m/s})}{2 \text{ kg} + 2 \text{ kg}}$$

$$= 1.5 \text{ m/s}$$

#5-8:



$$m_d = 1 \text{ kg} \quad m_b = 9 \text{ kg}$$

$$v_{di} = 10 \text{ m/s} \quad v_{bi} = 0 \text{ m/s} \quad v_f = ?$$

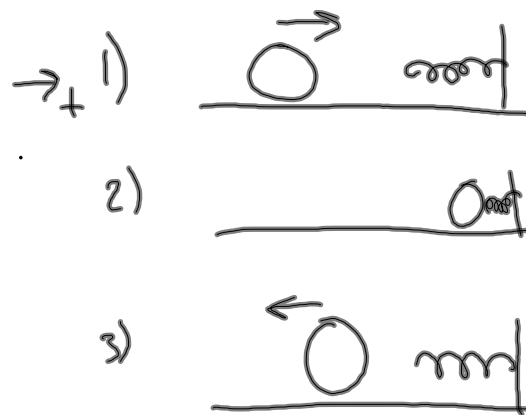
$$m_d v_{di} + \cancel{m_b v_{bi}} = (m_d + m_b) v_f$$

$$v_f = \frac{m_d v_{di}}{m_d + m_b}$$

$$= \frac{(1 \text{ kg})(10 \text{ m/s})}{(1 \text{ kg} + 9 \text{ kg})}$$

$$= 1 \text{ m/s}$$

#59:



a) momentum of ball

$$\begin{aligned}\bar{p} &= m \bar{v} \\ &= (8 \text{ kg})(2 \text{ m/s}) \\ &= 16 \text{ kg} \cdot \text{m/s}\end{aligned}$$

$$\begin{aligned}\text{b) } \Delta \bar{p} &= m \Delta \bar{v} \\ &= m (\bar{v}_f - \bar{v}_i) \\ &= (8 \text{ kg})(-2 \text{ m/s} - 2 \text{ m/s}) \\ &= -32 \text{ kg} \cdot \text{m/s}\end{aligned}$$

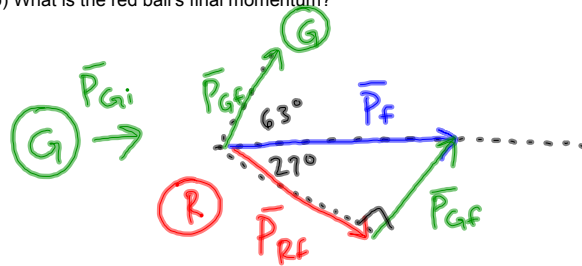
c) Impulse-Momentum Theorem

$$\begin{aligned}\bar{F} \Delta t &= m \Delta \bar{v} \\ \bar{F} &= \frac{m \Delta \bar{v}}{\Delta t} \quad \Delta t = 0.5 \text{ s} \\ &= \frac{-32 \text{ kg} \cdot \text{m/s}}{0.5 \text{ s}} \\ &= -64 \text{ N}\end{aligned}$$

HW Review and 2D Elastic Practice Problem 2.9.12 CP Physics

A green 5.00 kg ball moving 17.0 m/s hits a non-moving red 7.00 kg ball. After they hit, the red ball is moving to the right at a 27 degree angle from the green ball's original direction. The green ball is now moving at a 63 degree angle to the left of its original direction.

- a) What is the green ball's final velocity?
b) What is the red ball's final momentum?



$$\begin{aligned}\vec{P}_i &= \vec{P}_{Gi} + \vec{P}_{Ri} \\ &= m_G v_{Gi} = (5 \text{ kg})(17 \text{ m/s}) = 85 \text{ kg}\cdot\text{m/s}\end{aligned}$$

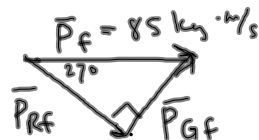
$$\vec{P}_f = \vec{P}_{Gf} + \vec{P}_{Rf}$$

↑ CANNOT simply add,
b/c they are vectors!

initial momentum = final momentum

$$\begin{aligned}\vec{P}_i &= \vec{P}_f \\ 85 \text{ kg}\cdot\text{m/s east} &= \vec{P}_f\end{aligned}$$

a) find $v_{Gf} \rightarrow$ find P_{Gf} first



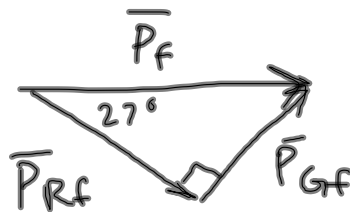
$$\sin(27^\circ) = \frac{P_{Gf}}{P_f}$$

$$\begin{aligned}P_{Gf} &= P_f \sin(27^\circ) \\ &= (85 \text{ kg}\cdot\text{m/s}) \sin(27^\circ) \\ &= 38.6 \text{ kg}\cdot\text{m/s}\end{aligned}$$

$$P_{Gf} = m_G v_{Gf}$$

$$v_{Gf} = \frac{P_{Gf}}{m_G} = \frac{38.6 \text{ kg}\cdot\text{m/s}}{5 \text{ kg}} = 7.71 \text{ m/s}$$

b) find p_{Rf}



$$\cos(27^\circ) = \frac{P_{Rf}}{P_f}$$

$$\begin{aligned} P_{Rf} &= P_f \cos(27^\circ) \\ &= (85 \text{ kg} \cdot \text{m/s}) \cos(27^\circ) \\ &= 75.7 \text{ kg} \cdot \text{m/s} \end{aligned}$$

Steps:

- 1) calculate initial momentum from ball that is moving
- 2) make a final momentum triangle
- 3) Use trigonometry to find each final momentum
- 4) use momentum to solve for velocity, if necessary

Main Concepts:

Impulse-Momentum

- Force, time, momentum

$$\vec{F} \Delta t = m \Delta \vec{v}$$

Cons. of Momentum

Elastic Collisions

Inelastic Collisions

1-D

2-D

1-D

2-D

$$m_1 \vec{v}_{1i} + m_2 \vec{v}_{2i} = m_1 \vec{v}_{1f} + m_2 \vec{v}_{2f}$$

$$\vec{p}_{1i} + \vec{p}_{2i} = \vec{p}_{1f} + \vec{p}_{2f}$$



objects apart, then stick together

$$m_1 \vec{v}_{1i} + m_2 \vec{v}_{2i} = (m_1 + m_2) \vec{v}_f$$

objects together, then move apart

$$(m_1 + m_2) \vec{v}_i = m_1 \vec{v}_{1f} + m_2 \vec{v}_{2f}$$